

1. Sampling, Quantization and Encoding (Criterion c) [40 points]

The waveform  $s(t)$  shown in Figure 1.1 is a segment of a voice signal that has a maximum frequency component at 4KHz and maximum amplitude of 2mV ( $M_{max} = -M_{min}$ ). Assume the signal is processed as described in the block diagram shown in Figure 1.2, answer the following:

- Determine the sampled signal values;  $m_s(nT)$ ,
- Determine the quantized signal values;  $m_q(nT)$ ,
- Determine the binary signal values;  $m_b$ ,
- Determine the output bit rate;  $R_b$ ,
- Calculate the Quantization Noise Power,  $Nq_{-2}$ ,
- If 3-bit Quantizer is used,
  - Calculate the new Quantization Noise Power;  $Nq_{-3}$ ,
  - Compare your  $Nq_{-3}$  with the answer of part e,
- If the input waveform  $s(t)$  has a maximum frequency component of 1KHz, determine the new quantized values of  $m_s(nT)$ ,
- Why do we use anti-aliasing filter?

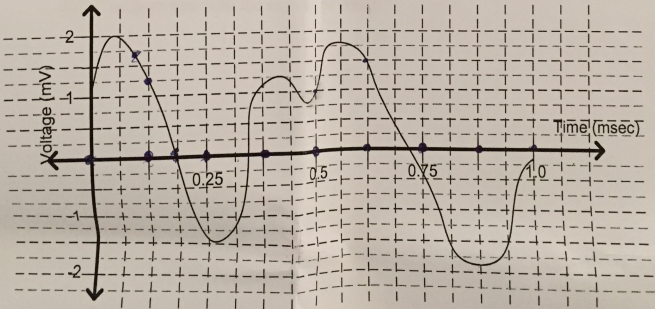


Figure 1.1:  $s(t)$  waveform

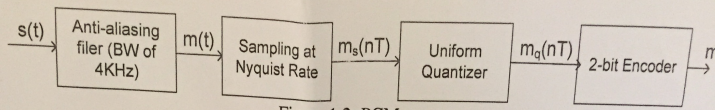


Figure 1.2: PCM system

Q2. Signal Sampling in the frequency domain [10 point]

The signal  $s(t)$  given below is ideally sampled at a rate 4000 Hz and then passed through a LPF,

$$s(t) = \cos(2\pi \times 1000 \times t) + \cos(2\pi \times 2000 \times t + \pi)$$

- Plot the amplitude spectrum of the sampled signal,
- What is the output signal if the filter bandwidth is 1000 Hz?

Q3. Decision Region and Optimal Receiver Design [30 point]

A discrete memory-less source output the information bits "0" and "1" with equal probability. Assume the information bit "0" is modulated by symbol " $S_1$ " and information bit "1" is modulated by symbol " $S_2$ " as shown in Figure 2. Assume the noise power density  $\frac{N_0}{2} = 4 \times 10^{-9} V^2/Hz$  answer the following:

- Determine the optimal receiver decision criteria, ✓
- Sketch the decision regions for both symbols, ✓
- Calculate the probability of error at receiver (symbol error), ✓
- Draw the block diagram of the correlate optimum receiver [clearly label each block], ✓
- Draw the block diagram of the match filter optimum receiver [clearly label each block], ✓
- Assume probability of transmitting bits "0" is 10 times the probability of transmitting bit "1" ( $P("0") = 10P("1")$ )
  - Determine the optimal receiver decision criteria. ✓
  - Compare this with the answer of part a.

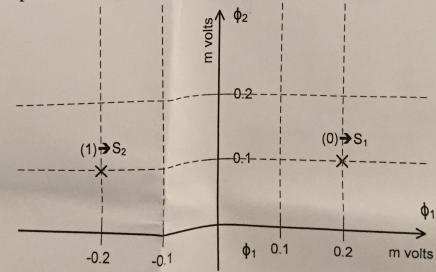


Figure 2

Good Luck